



Short communication

Improvement quantum capacitance in supercapacitors using vacancy-defected BC₃ monolayer

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ABSTRACT

In present research, we aimed to assess effectiveness of employing defected BC₃ monolayer in supercapacitors as an electrode through DFT computations. Our focus was on single and double-vacancy BC₃ monolayer. We studied stored charge diagrams, integrated quantum capacitance (C_Q), and density of state (DOS) for both pristine and vacancy-modified defected BC₃ monolayer structures. According to findings, applying vacancy-modified defected structures between -0.80 and 0.80 V leads to greater C_Q value in comparison to pristine BC₃ monolayer. Single and double vacancies may be employed as positive and negative electrodes, and are considered as a semiconductor. Computations reveal that stored charge in vacancy-modified defected structures is more than pristine BC₃ monolayer between 0 and 0.8 V. Moreover, DV-modified defected structure stores more charge than both SV structures and BC₃ monolayer. Our findings suggest that DV BC₃ monolayer shows potential as a material for high-performance supercapacitors.

1. Introduction

Over past decade, demand for portable and compact electronic devices has spurred significant interest in creating sustainable energy storage systems. Despite their widespread use, Li-ion batteries (LIBs) have notable shortcomings such as high maintenance costs, short lifespan, and low power density [1–4]. As an alternative, supercapacitors have gained traction as a promising option due to their inherent advantages, including rapid charging/discharging rates, long cycle life, and remarkable power density [5–11]. At present, the main type of supercapacitor, or electrochemical double-layer capacitor (EDLC), utilizes carbon electrodes adsorbing ions from electrolytes during charging and releasing them upon discharge, thereby allowing for quick and reliable cycles of charge and discharge. The ideal electrode for a supercapacitor should possess several desirable qualities, such as

chemical stability to ensure a long lifespan, a large surface area that is easily accessible, strong electrical conductivity, and high specific capacitance. As a result, there have been significant recent efforts focused on developing novel electrode materials and architectures that can improve the performance of supercapacitors [12–14].

For conventional EDLCs, energy storage capabilities are primarily determined by supercapacitor total capacitance (C_T), which is derived from combined contributions of double-layer capacitance (C_D) and electrode quantum capacitance (C_Q). This relationship can be expressed as $1/C_T = 1/C_Q + 1/C_D$ [12,13,15]. Inherent electronic structures of electrode material are the main factor that determines C_Q [16,17], whereas C_D relies on electrode–electrolyte interfacial structure [18–20]. Previous investigations [21–24] have aimed to improve total capacitance by focusing on C_D, achieved by developing porous based materials for electrode with in pore size lower of solvated ions (~1 nm), to

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facilitate movement of ions from electrolyte to electrode [25]. Hwang's research group [12] proposed that C_Q is a critical factor in determining total capacitance, leading to considerable efforts being devoted towards enhancing C_Q . Accordingly graphene, which is a 2D hexagonal carbon with sp^2 hybridization, has been extensively studied electrodes [26,27]. According to former reports, practical use of pristine graphene is limited due to low C_Q , which is caused by absence of DOS at Fermi level [28]. Different approaches were proposed to enhance its quantum capacitance, such as utilizing tensile strain and surface rippling [28], introducing vacancies [29], functionalization [30], and chemical doping [31,32].

Due to beneficial characteristics, including thermal stability, low cost, excellent electrical conductivity, and outstanding surface area ($2630 \text{ m}^2 \text{ g}^{-1}$), graphene and its derivatives have been utilized as electrodes [33–37]. Various investigations have shown that modifying graphene through functionalization, introducing defects, and doping or co-doping can be successful approaches for enhancing its C_Q [38]. Introduction of certain substituted groups (e.g. benzene, $-\text{NH}_2$, and $-\text{H}$) through functionalization can have a considerable impact on enhancing energy density (E) and C_Q of graphene [30,39–41]. According to theoretical studies, Stone Wales, di-interstitials, and di-vacancies defects can enhance C_Q of graphene more than pristine graphene due to presence of quasi-localized states close to Fermi level caused by these defects [42]. To increase C_Q of electrodes made from graphene, dopants, surface rippling, strain, and defects are suggested as effective techniques for modifying carbon-based electrodes [29,43–48]. After analyzing studies on pristine and doped graphene with positive powers, it has been discovered that doped systems deliver favorable characteristics as efficient electrodes [49].

BC₃, consisting of a single layer of N and C atoms, shares many similarities with graphene [50–53]. However, it has advantages over graphene, such as a higher-band gap and stronger spin–orbit coupling [54]. The aim of present research was to improve C_Q of BC₃ by introducing vacant areas in monolayer structure. We also sought to optimize the performance of these vacancy-modified BC₃ structures and evaluate their effectiveness as electrodes in supercapacitors. By examining impact of atom vacancies on C_Q and electronic structure of BC₃-based supercapacitors, we aimed to enhance efficacy of electronic storage systems.

2. Computational approach

To conduct DFT computations, GAMESS software has been utilized [55]. Moreover, B3LYP functional was employed that has been augmented with an empirical dispersion term (B3LYP-D) to enhance its accuracy in calculating noncovalent interactions. Previous research has demonstrated that the B3LYP functional is effective in reproducing experimental attributes and has been commonly utilized in investigations of nanostructures [56,57]. Additionally, it has been shown to be a reliable method for calculating III-V semiconductors [58].

To generate stored charge diagrams for both pristine and defected BC₃, integrated quantum capacitance, and gravimetric DOS diagrams, subsequent equations in numerical computations have been employed. C_{total} of electrodes can be represented as below:

$$\frac{1}{C_{\text{total}}} = \frac{1}{C_{\text{DL}}} + \frac{1}{C_Q} \quad (1)$$

Herein, double-layer capacitance is represented by C_{DL} and quantum capacitance is indicated by C_Q . Total capacity of BC₃-based supercapacitors has determined by C_Q rather than C_{DL} . This means that if changes are made to electrode structure that result in an enhancement in C_Q , total capacity of supercapacitor will also increase [12]. Differential quantum capacitance (C_Q^{diff}) is computed as below [59]:

$$C_Q^{\text{diff}} = e^2 \int_{-\infty}^{+\infty} D(E) F_T(E - \mu) dE \quad (2)$$

Electrochemical potential μ , expressed by equation $\mu = e\Phi$, where e represents elementary electric charge, can rigidly modify local potential Φ . In Equation (2), relative energy with respect to Fermi level and density of states (1/eV) are represented by E and $D(E)$, respectively. Function of thermal broadening (F_T) is determined as below:

$$F_T = \frac{1}{4k_B T} \left(\frac{E}{2k_B T} \right)$$

Herein, Boltzmann constant is indicated by k_B and temperature is represented by T (300 K). Integrated C_Q (C_Q^{int}) can be computed based on following equation [12,31,60,61]:

$$C_Q^{\text{int}} = \frac{1}{V_e} \int_0^V C_Q^{\text{diff}}(V') dV'$$

3. Results and discussion

3.1. Electronic and structural attributes of pristine and vacancy-modified BC₃ monolayer

Initially, structural attributes of pristine BC₃ monolayer were optimized and documented. Subsequently, two kinds of vacancies were optimized based on previous investigation: single vacancy (SV) and double vacancy (DV). DOS diagrams for all structures were then computed. Eventually, stored charge diagrams, C_Q^{int} , gravimetric C_Q^{int} , DOS, and gravimetric DOS of both pristine and vacancy-modified BC₃ monolayers were presented.

To analyze electronic and structural attributes of pristine and vacancy-modified defected BC₃ monolayer, optimization has been performed. C–B bond distance was found to be around 1.42 Å, while C–C bond distance was around 1.57 Å. This result was in line with previous experimental and theoretical studies [62]. Pristine BC₃ monolayer had a smaller band gap that was located close to Fermi level. However, presence of defects caused band gap in pristine BC₃ monolayer to increase [51,62].

Two varieties of vacancies or defects were examined over surface of BC₃ monolayer, and its structures are presented in Fig. 1. Vacancy defects have been investigated widely as a type of point defect, and their effects on physicochemical attributes of nanostructures have been explored [63]. When an atom is lost from a lattice site, a “vacancy” or Schottky defect is created [63]. SV and DV are significant defects that result from a missing atom in their conventional atomic site. It is important to note that vacancies are typically formed during solidification as a result of atoms' vibration and local rearrangement [63]. Band gap values of single and double vacancy of BC₃ were computed, and outcomes were found to be lower than those of pristine BC₃ monolayer. DOS diagrams of vacancy-modified defected BC₃ monolayer are displayed in Fig. 2. Following an enhancement in quantity of absent atoms and enlargement of cavity in BC₃ monolayer, electronic states with lower energy levels were occupied by cavities and electrons. This resulted in a reduction in height of peaks and a shift of diagrams towards conduction band. Maximum peak range for total DOS diagrams increased from 3 to 5 eV. Accordingly, unlike pristine BC₃ monolayer, defected BC₃ monolayer became a p-type semiconductor.

3.2. Computation C_Q of pristine and vacancy-modified BC₃ monolayer

The BC₃ monolayer has potential applications as an electrode in supercapacitors. Former studies have shown that C_Q is linked to DOS that in turn is connected to charge. The Fermi surface energy value in pristine BC₃ is equal to -5.04 electron volts. The Fermi surface energy value in samples with single and double defects is equal to -4.86 and

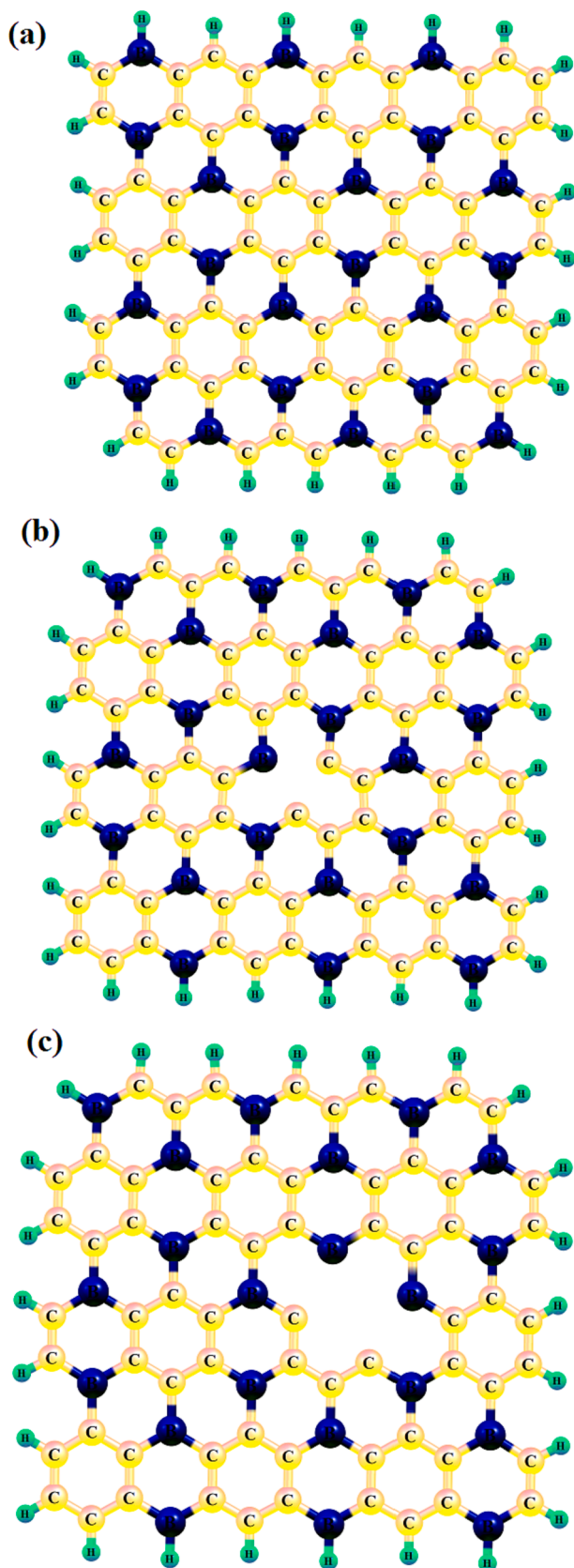


Fig. 1. The proposed BC₃ monolayer models including (a) pristine, (b) single-vacancy, and (c) double-vacancy BC₃ monolayer.

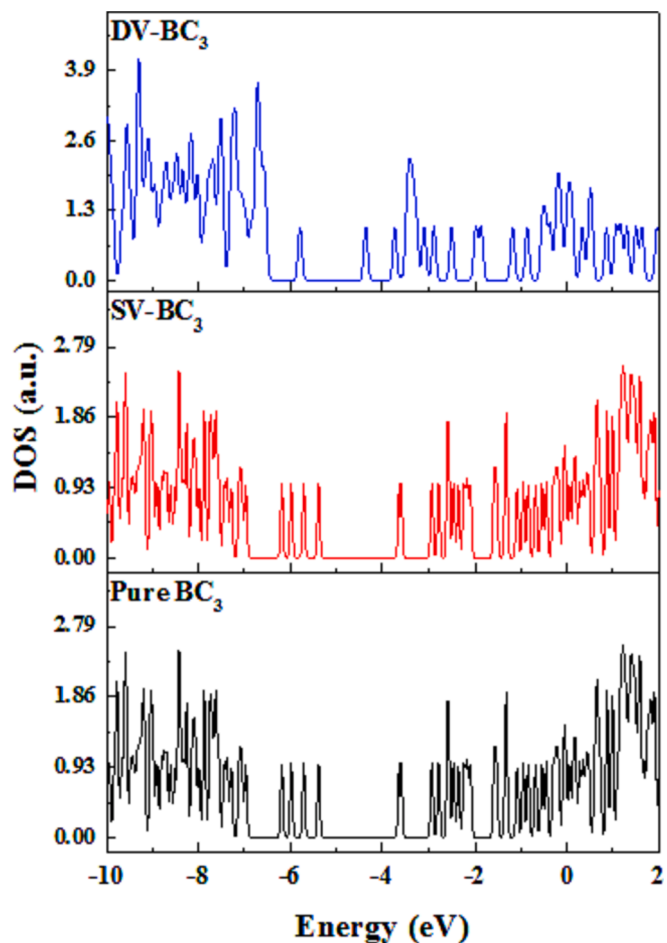


Fig. 2. DOS plots of the (a) pristine, (b) single-vacancy, and (c) double-vacancy BC₃ monolayer.

−4.21 electron volts, respectively. Moreover, Fig. 2 provided an illustration of the total DOS (TDOS) of both unmodified and modified BC₃. It was observed that the band gap of modified BC₃ (SV = 1.94 eV) and DV = 1.53 eV) was lower than that of BC₃ (2.17 eV), which was a semiconductor. In the case of modified BC₃, certain DOS peaks surpassed the Fermi Level, indicating conductor-like behavior attributed to the presence of unpaired electrons. Yang's research group have indicated that SV defects have a significant impact on improving C_Q of BC₃ monolayer owing to presence of localized states close to Fermi level. Models of SV graphene with varying vacancy concentrations exhibit superior C_Q results compared to pristine graphene. C_Q values (measured in F/cm²) were noted for two different varieties of DV: (5-8-5) and (555-777). C_Q of structures between −1.50 and 1.50 V is greater than that of bare graphene [64]. Utilizing DFT, it was found that C_Q of SV BC₃ monolayer enhanced owing to attendance of localized states close to Fermi level. Fig. 3 are shown in the gravimetric DOS diagrams for both pristine and vacancies BC₃ monolayer. To obtain DOS, density of states for pristine material can be divided by its molecular weight. Defects in monolayer cause peaks to appear with higher intensity between −0.80 and 0.80 V, as a result of an increase in localized states close to Fermi level. Impurity states observed close to Fermi level in density of states diagrams of defected modified BC₃ were attributed to p orbitals of atoms involved in defect. Enhancement in number of orbitals has a significant impact on altering energy of Fermi level. These impurity states serve as a foundation for enhancing C_{total} and C_Q.

Fig. 4 displays computed C_Q values for pristine BC₃ monolayer and vacancy-modified defected BC₃ monolayer structures (SV and DV) over −0.80 to + 0.80 V (electrochemical range for aqueous electrolytes). As

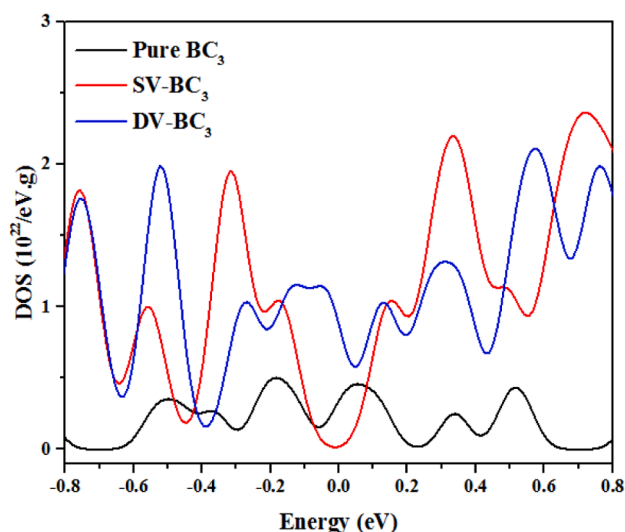


Fig. 3. Gravimetric DOS plots of the (a) pristine, (b) single-vacancy, and (c) double-vacancy BC_3 monolayer.

anticipated, defects altered attributes of pristine BC_3 monolayer structure and had a significant impact on C_Q diagrams, with each structure exhibiting optimal performance at a specific potential. Compared to pristine BC_3 monolayer, vacancy-modified defected BC_3 monolayer structures exhibit asymmetric behaviors, but show a considerable increase in positive and negative potentials within a certain range. Quantum capacitance was found to enhance with an increment in defects concentration and number of missing atoms [65].

Fig. 4 indicates C_Q^{int} values of vacancy-modified defected and pristine BC_3 monolayer. Findings indicate that C_Q of BC_3 monolayer with vacancy modification and defects is greater than pristine BC_3 monolayer within -0.80 to 0.80 V. Compared to pristine BC_3 monolayer at 0 V, quantum capacitance of all structures exhibited enhancement. Upon

closer examination, it was observed that CQ value of DV showed a remarkable improvement over other structures at high voltages from 0 to 0.80 V. Based on information obtained from Fig. 4, it can be concluded that DV performs well and can serve as a positive electrode. The amount of charge stored in a BC_3 monolayer, both in its pristine form and with vacancy modification and defects between -0.80 and $+0.80$ V are indicated in Fig. 5. Compared to pristine BC_3 monolayer, capability to store electric charges at positive voltages enhances. As shown in Fig. 4, stored charge diagrams for defect structures exhibit an increment in positive voltages compared to pristine BC_3 monolayer. Comparing different structures, DV exhibits the best performance between 0 and 0.80 V, with a significant increase in stored charge compared to pristine BC_3 monolayer, as shown in Fig. 5. Between -0.80 and 0 V, pristine BC_3 monolayer has a higher stored charge than defective structures. At 0 V, all structures have a stored charge value of 0 V, similar to that of pristine BC_3 monolayer.

4. Conclusion

Density functional theory computations were utilized to explore potential of BC_3 monolayers as electrode materials for supercapacitors. We proposed an approach to increase quantum capacitance of BC_3 by introducing appropriate vacancy defects. The creation of vacancies had a remarkable impact on electronic structure and DOS of BC_3 monolayer. Specifically, the defect resulted in increased energy levels in p molecular orbitals of atoms involved, as well as an increase in total capacitance and available quantum capacitance of supercapacitor. Among the structures investigated, DV configuration showed the most promising results, with a theoretical C_Q value of up to 657 F/g at positive electrode. These findings indicate that vacancy-modified defected BC_3 structures could serve as effective electrode materials for supercapacitors.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence

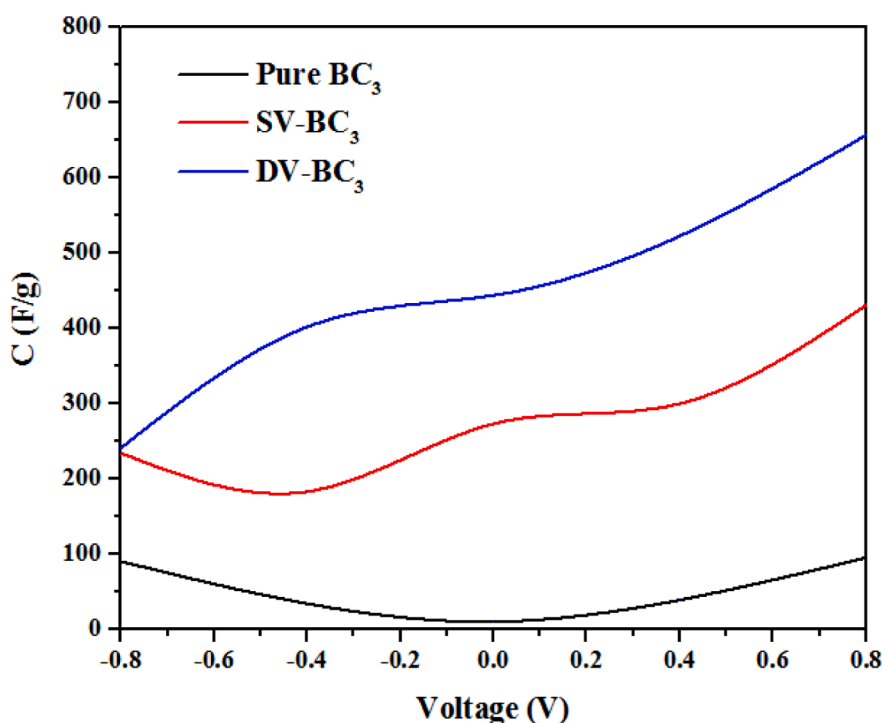


Fig. 4. Integrated quantum capacitance of the pristine, single-vacancy, and double-vacancy BC_3 monolayer.

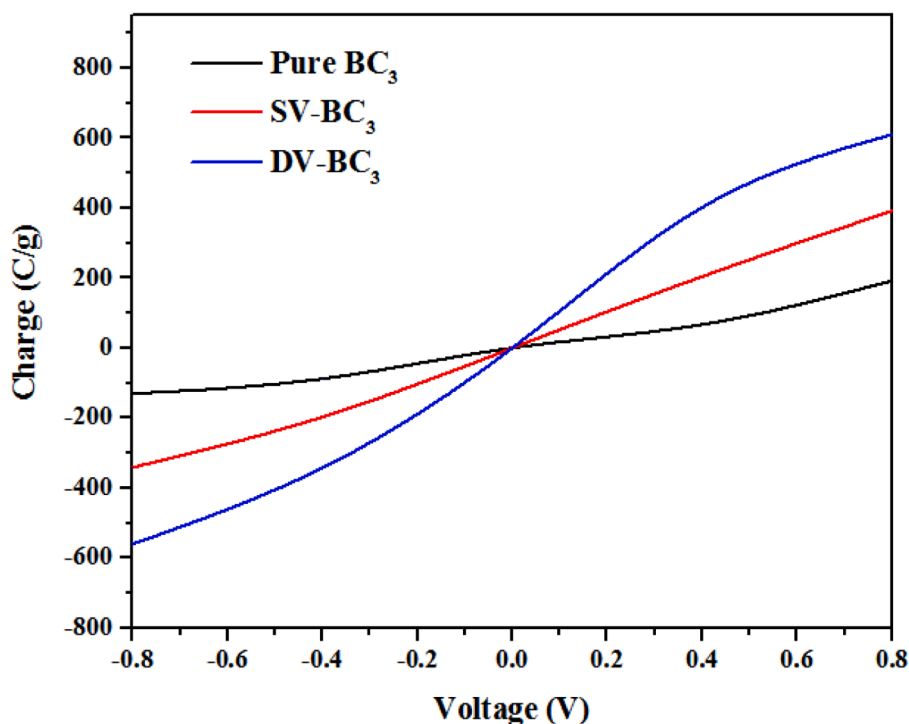


Fig. 5. Calculated stored charge of the pristine, single-vacancy, and double-vacancy BC₃ monolayer.

the work reported in this paper.

Data availability

No data was used for the research described in the article.

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